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Cuckoo Search Algorithm: An Introduction

Presentation · April 2020

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Nature-Inspired Optimization Algorithms View project

Cuckoo Search: An Introduction

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For details, please read my book:

Nature-Inspired Optimization Algorithms, Elsevier, (2014).

Matlab codes are downloadable from https://uk.mathworks.com/matlabcentral/profile/authors/3659939-xs-yang

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Almost Everything is Optimization

Almost everything is optimization ... or needs optimization ...

- Maximize efficiency, accuracy, profit, performance, sustainability, ...
- Minimize costs, wastage, energy consumption, travel distance/time, CO₂ emission, impact on environment, ...

Mathematical Optimization

Objectives: maximize or minimize $f(x) = [f_1(x), f_2(x), ..., f_m(x)],$

$$\boldsymbol{x} = (x_1, x_2, \dots, x_D) \in \mathbb{R}^D,$$

subject to multiple equality and/or inequality design constraints:

$$h_i(\boldsymbol{x}) = 0, \quad (i = 1, 2, ..., M),$$

$$g_j(\boldsymbol{x}) \le 0, \quad (j = 1, 2, ..., N).$$

In case of m = 1, it becomes a single-objective optimization problem.

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Cuckoo Search

Optimization problems can usually be very difficult to solve, especially large-scale, nonlinear, multimodal problems.

In general, we can solve only 3 types of optimization problems:

- Linear programming
- Convex optimization
- Problems that can be converted into the above two

Everything else seems difficult, especially for large-scale problems. For example, combinatorial problems tend to be really hard – NP-hard!

Deep Learning

The objective in deep nets may be convex, but the domain is not convex and it's a high-dimensional problem.

Minimize
$$E(\boldsymbol{w}) = \frac{1}{n} \sum_{i=1}^{n} \left[u_i(\boldsymbol{x}_i, \boldsymbol{w}) - \bar{y}_i \right]^2$$
,

subject to various constraints.

Key Components for Optimization



Optimization Techniques

There are a wide spectrum of optimization techniques and tools.

Traditional techniques

- Linear programming (LP) and mixed integer programming.
- Convex optimization and quadratic programming.
- Nonlinear programming: Newton's method, trust-region method, interior point method, ..., barrier Method, ... etc.

But most real-world problems are not linear or convex, thus traditional techniques often struggle to cope, or simply do not work...

New Trends – Nature-Inspired Metaheuristic Approaches

- Evolutionary algorithms (evolutionary strategy, genetic algorithms)
- Swarm intelligence (e.g., ant colony optimization, particle swarm optimization, firefly algorithm, cuckoo search, ...)
- Stochastic, population-based, nature-inspired optimization algorithms

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The Essence of an Algorithm

Essence of an Optimization Algorithm

To generate a better solution point $x^{(t+1)}$ (a solution vector) from an existing solution $x^{(t)}$. That is, $x^{(t+1)} = A(x^{(t)}, \alpha)$ where α is a set of parameters.



Population-based algorithms use multiple, interacting paths.

Different algorithms Different ways for generating new solutions!

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Main Problems with Traditional Algorithms

What's Wrong with Traditional Algorithms?

- Traditional algorithms are mostly local search, thus they cannot guarantee global optimality (except for linear and convex optimization).
- Results often depend on the initial starting points (except linear and convex problems). Methods tend to be problem-specific (e.g., *k*-opt, branch and bound).
- Struggle to cope problems with discontinuity.

Nature-Inspired Optimization Algorithms

Heuristic or metaheuristic algorithms (e.g., ant colony optimization, particle swarm optimization, firefly algorithm, bat algorithm, cuckoo search, differential evolution, flower pollination algorithm, etc) tend to be a global optimizer so as to

- Increase the probability of finding the global optimality (as a global optimizer)
- Solve a wider class of problems (treating them as a black-box)
- Draw inspiration from nature (e.g., swarm intelligence)

But they can be potentially more computationally expensive.

Cuckoo Search

Cuckoo search (CS) was developed by Xin-She Yang and Suash Deb in 2009.



Cuckoo brood parasitism

- 59 cuckoo species (among 141 cuckoo species) engage the so-called obligate reproduction parasitism strategy.
- Cuckoos lay eggs in the nests of host birds (such as warblers) and let host birds raise their chicks.
- Eggs may be discovered/abandoned with a probability ($p_a \approx 0.25$).
- Co-evolutionary arms race between cuckoo species and host species.

Cuckoo Behaviour (BBC Video)

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Cuckoos' Behaviour and Idealization (Yang and Deb, 2009)

- Each cuckoo lays one egg at a time and dumps it in a randomly chosen nest.
- The best nests with high-quality eggs will be carried over to the next generations.
- The number of available host nests is fixed, and the egg laid by a cuckoo is discovered by the host bird with a probability $p_a \in (0, 1)$. In this case, the host bird can either get rid of the egg or simply abandon the nest and build a completely new nest elsewhere.



Here, x_i is the solution vector (or position of nest *i*) in the search space at iteration *t*, and α is a scaling factor. $L(s, \lambda)$ is the step size to be drawn from the Lévy distribution with an exponent λ .

Cuckoo Search (CS) (Yang and Deb, 2009)

Two search mechanisms in CS: local random walks and global Lévy flights.

Local random walks:

$$\boldsymbol{x}_i^{t+1} = \boldsymbol{x}_i^t + s \otimes H(p_a - \epsilon) \otimes (\boldsymbol{x}_j^t - \boldsymbol{x}_k^t).$$

 $[x_i, x_j, x_k \text{ are 3 different solutions, } H(u) \text{ is a Heaviside function, } \epsilon \text{ is a random number drawn from a uniform distribution, and } s \text{ is the step size.}$

Global random walks via Lévy flights:

$$\boldsymbol{x}_i^{t+1} = \boldsymbol{x}_i^t + \alpha L(s,\lambda), \quad L(s,\lambda) \sim \frac{\lambda \Gamma(\lambda) \sin(\pi \lambda/2)}{\pi} \frac{1}{s^{1+\lambda}}, \ (s \gg s_0).$$

Generation of new moves by Lévy flights, random walks and elitism.

The switch between these two search mechanisms is governed by the discovery probability $p_a = 0.25$.

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Mathematical Foundation for Cuckoo Search

Isotropic andom walks (diffusion) Gaussian distribution Lévy flights (superdiffusion) Lévy distribution

$$p(s) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{(s-\mu)^2}{2\sigma^2}\right], \qquad L(s,\lambda) \sim \frac{1}{\pi} \int_0^\infty \cos(ts) e^{-\alpha t^\lambda} dt.$$

Typical paths of t = 50 consecutive steps of random walks



Typical Parameter Values

- Population size: n = 10 to 40 (up to 100 if necessary).
- Lévy exponent: $\lambda = 1.5$.
- $\alpha = O(L/100)$ to O(L/10) where L is the typical scale of the problem. Typically, we can use $\alpha = 0.01$ to 0.1 for function optimization.
- Number of iterations $t_{\rm max} = 500$ to 1000.

Pseudo-random step size (s) for Lévy flights

Quite tricky to generate, though Mantegna's algorithm works well.

$$s = \frac{U}{|V|^{1/\lambda}}, \quad U \sim N(0, \sigma^2), \quad V \sim N(0, 1),$$

where '~' means 'to draw' random numbers from the probability distribution on the right-hand side. The variance σ^2 is calculated by

$$\sigma^{2} = \left[\frac{\Gamma(1+\lambda)}{\Gamma((1+\lambda)/2)} \cdot \frac{\sin(\pi\lambda/2)}{\lambda 2^{(\lambda-1)/2}}\right]^{1/\lambda},$$

where $\Gamma(\nu)$ is the standard Gamma function. For example, if $\lambda = 1$, we have $\sigma^2 = 1$ since $\Gamma(1 + \lambda) = 1$, $\Gamma((1 + \lambda)/2) = 1$ and $\sin(\pi/2) = 1$.

Cuckoo Search Pseudocode

Algorithm 1: Cuckoo Search **Data:** Objective functions f(x)Result: Best or optimal solution 1 Initialization of parameters $(n, p_a, \lambda \text{ and } \alpha)$; 2 Generate initial population of n host nests x_i ; 3 while (t < MaxGeneration) or (stop criterion) do Get a cuckoo randomly: 4 Generate a solution by Lévy flights; 5 Evaluate its solution quality or objective value f_i ; 6 Choose a nest among n (say, j) randomly; 7 if $(f_i < f_j)$ then 8 Replace j by the new solution i; 9 end 0 A fraction (p_a) of worse nests are abandoned; .1 New nests/solutions are built/generated; .2 Keep best solutions (or nests with quality solutions); .3 Rank the solutions and find the current best solution; 4 .5 Update $t \leftarrow t + 1$; 6 end

CS is very efficient

Cuckoo Search Demo: Highly Efficient!

Rosenbrock (banana) function

$$f(x,y) = (1-x)^2 + 100(y-x^2)^2, \quad (x,y) \in \mathbb{R}^2.$$



Cuckoo Search (Demo video at Youtube) [Please click to start]

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Multi-objective Cuckoo Search (MOCS)

For example, the so-called ZDT function with D = 30 dimensions

minimize $f_1(x) = x_1$, and $f_2(x) = g(x)h(x)$, $x \in [0,1]^{30}$,

where

$$g(\boldsymbol{x}) = 1 + rac{9}{29} \sum_{j=2}^{D=30} x_j, \quad h(\boldsymbol{x}) = 1 - \sqrt{rac{f_1}{g}} - rac{f_1}{g} \sin(10\pi f_1),$$

has a nonconvex Pareto front in the domain $0 \le x_i \le 1$ where i = 1, 2, ..., 30.



Cuckoo Search (Demo Codes) and References

CS Demo Codes

- The standard CS demo in Matlab can be found at the Mathswork File Exchange https://uk.mathworks.com/matlabcentral/fileexchange/74767-the-standard-cuckoo-search-cs
- The multi-objective cuckoo search (MOCS) code is also available at https://uk.mathworks.com/matlabcentral/fileexchange/74752-multiobjective-cuckoo-search-mocs

Some References

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